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What season suits you best? Seasonal light changes and cyanobacterial competition

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Nearly all living organisms, including some bacterial species, exhibit biological processes with a period of about 24 h called circadian (from the Latin *circa*, about and *dies*, day) rhythms. These rhythms allow living organisms to anticipate the daily alternation of light and darkness. Experiments carried out in cyanobacteria have shown the adaptive value of circadian clocks. In these experiments, a wild type cyanobacterial strain (with a 24 h circadian rhythm) and a mutant strain (with a longer or shorter period) grow in competition. In different experiments, the external light dark cycle was chosen to match the circadian period of the different strains, revealing that the strain whose circadian period matches the light-dark cycle has a larger fitness. As a consequence, the initial population of one strain grows while the other decays. These experiments were made under fixed light and dark intervals. In Nature, however, this relationship changes according to the season. Therefore, seasonal changes in light could affect the results of the competition. Using a theoretical model, we analyze how modulation of light can change the survival of the different cyanobacterial strains. Our results show that there is a clear shift in the competition due to the modulation of light, which could be verified experimentally.

I. Introduction

Circadian rhythms, oscillations with approximately 24 h period in many biological processes, are found in nearly all living organisms. Until the mid-1980s, it was thought that only eukaryotic organisms had a circadian clock, since it was assumed that an endogenous clock with a period of $\tau = 24$ h would not be useful to organisms that often divide more rapidly [1]. However, in 1985, several research groups discovered that in cyanobacteria there was a daily rhythm of nitrogen fixation [2–4]. Huang and co-workers were the first to recognize that a strain of Synechococcus, a unicellular cyanobacterium, had circadian rhythms [5]. This transformed Synechococcus in one of the simplest models for studying the molecular basis of the circadian clock.

The ubiquity of circadian rhythms suggests that they confer an evolutionary advantage. The adaptive functions of biological clocks are divided into two hypotheses. The external advantage hypothesis supposes that circadian clocks allow living organisms to anticipate predictable daily changes, such as light/dark, so they can schedule their biological functions like feeding and reproduction at appropriate times. In contrast to this hypothesis, it has been suggested that circadian clocks confer adaptive benefit to organisms through temporal

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coordination of their internal physiology (intrinsic advantage) [6]. In this case, the circadian clock should be of adaptive value in constant conditions as well as in cyclic environments.

In order to study if circadian clocks provide evolutionary advantages, Woelfle and co-workers tested the relative fitness under competition between various strains of cyanobacteria [7]. They carried out experiments where a wild-type strain $(\tau = 25 \text{ h})$ of cyanobacteria and mutant strains, with shorter ($\tau = 22$ h) and longer ($\tau = 30$ h) periods, were subjected to grow in competition with each other under light-dark (LD) cycles of different periodicity. They found that the strain which won the competition was the one whose free-running period matched closely the period of the LD cycle. This difference in fitness was observed despite the fact that the growth rates were not significantly different when each strain was grown with no competition. Also, mutant strains could outcompete wild-type strains under continuous light (LL) conditions, suggesting that endogenous rhythms are advantageous only in rhythmic environments [7]. This study provided one of the most convincing evidence so far in support of fitness advantages of synchronization between the endogenous period and the period of environmental cycles.

Ouyang et al. [8] suggested an explanation for fitness differences: this could be due to competition for limiting resources or secretion of diffusible factors that inhibit the growth of other cyanobacterial strains. Roussel et al. [9] proposed mathematical models in order to test which of these hypotheses was more plausible. They found that the model based on mutual inhibition was consistent with the experimental observations of [8]. In this model, the mechanism of competition between cells involves the production of a growth inhibitor, which is produced only during the subjective day (sL) phase, and that growth occurs only in the light phase.

Each of the experiments and computational simulations mentioned before had equal amounts of light and dark exposure. However, in Nature the relationship is not constant, and the duration of sunlight in a day changes according to the season and the latitude. The circadian system has to adapt to day length variation in order to have a functional role in optimizing seasonal timing and generating the capacity to survive at different latitudes [10]. Using this as a motivation, we will test how day length variation plays a role in the competition between different strains of cyanobacteria.

II. The model

For modeling the growth of each cyanobacterial strain, we use the model introduced by Gonze et al. [11] that is based on a diffusible inhibitor with a light sensitive oscillator to represent the cellular circadian oscillator. The evolution equations of cell population N_i and the level of inhibitor I are:

$$\frac{dN_i}{dt} = k_i N_i \left(1 - \sum_{j=1}^n N_j\right),$$
$$\frac{dI}{dt} = \sum_{i=1}^n N_i \left(p_i - \frac{V_{max}I}{K_M + I}\right)$$
(1)

$$k_{i} = \begin{cases} k & \text{in L and } i \text{ in sL or } I < I_{c} \\ 0 & \text{otherwise,} \end{cases}$$

$$p_{i} = \begin{cases} p & \text{if } i \text{ in sL} \\ 0 & \text{otherwise.} \end{cases}$$
(2)

In these equations, N_i is the number of cells of strain i, k_i is the growth rate of each strain, p measures the rate of inhibitor production, V_{max} is the maximum rate and K_M is the Michaelis constant characterizing the enzymatic degradation of the inhibitor.

Following the work of Gonze et al., we use a modified version of the Van der Pol oscillator to produce sustained circadian oscillations [11]. This simple mathematical model can describe circadian oscillations.

$$\frac{dx}{dt} = 24\frac{\pi}{12}(x_c + 0.13(\frac{x}{3} + \frac{4}{3}x^3 - \frac{256}{105}x^7) + B(t)),\\ \frac{dx_c}{dt} = 24\frac{\pi}{12}(-x(\frac{24}{\tau_x})^2 + \frac{B(t)}{3}x_c - 0.15B(t)x) \quad (3)$$

with

$$B(t) = (1 - \frac{x}{3})0.39\rho^{0.23},$$

$$\rho = \begin{cases} 5 & \text{in light phase (L),} \\ 0 & \text{in dark phase (D).} \end{cases}$$
(4)



Figure 1: Following the schematic explanation of Gonze et al. [11], we show how the model works. The inhibitor I is produced in 3, during the sL phase, and it is degraded during the entire day. Each strain grows in 1, if its sD phase overlaps with L and $I < I_c$, and in 2, when its SL phase overlaps with L.

These phenomenological equations produce oscillations in the circadian variable x with a period close to τ_x . x_c is a complementary variable and B(t) represents the coupling between the external LD cycle and the circadian oscillator, which depends on the light intensity ρ . We use this simple and phenomenological model because the detailed mechanisms, both at molecular and population level, have remained unknown in Synechococcus elegantus. For example, it is still unclear which phospho-state of kaiC, one of the clock genes identified in this organism, is involved in activation or suppression due to inconsistent reports. There are different mathematical models proposed for the molecular mechanisms of Synechococcus, but none of them has been experimentally verified [14]. We chose the model by Gonze et al [11] since the parameters on their equations are in agreement with the experimental data obtained by Woelfle et al. [7]. These values are $V_{max} = 1000, k = 1.8,$ $I_c = 0.01, p = 500 \text{ and } K_M = 0.05.$

In Fig. 1, we present a schematic plot of the model that shows how the growth of each population is coupled with the circadian oscillator. As it can be seen in this figure, when we modify the length of the light (L) phase then the overlaps 1 and 2 change, so the growth of each strain is altered affecting the competition. This effect is due to the fact that each strain grows always when its subjective phase sL overlaps the external light phase (2),



Figure 2: Day length over the course of 2012 at different latitudes in South America.

and when sD overlaps L only if the inhibitor is below a threshold I_c (1). The inhibitor is secreted in the sL phase and then it is degraded.

III. Results

In many organisms, a photoperiodic response is reflected in a physiological change. Photoperiodic responses are common among organisms from the equator to high latitudes and have been observed in different types of organisms, from arthropods to plants. Diapause (a suspension of development done by insects), migration and gonadal maturation are examples of these annual changes controlled by photoperiod. These biological processes are triggered as soon as the day length reaches certain duration, known as the critical photoperiod. Even near the equator, where day length changes are very small through the whole year, they are used to synchronize reproductive activities with annual events.

In Fig. 2, we show how day length varies depending on the latitude [13]. The figure compares the day length on the twenty-first day of each month in three cities in South America. We show Quito (Ecuador), which sits near the equator in latitude $0^{\circ}15'$, Jujuy (Argentina), which is located near the tropic of Capricorn in latitude $24^{\circ}01'$ and Ushuaia, the southernmost city in Argentina which



Figure 3: (A) The outcome of competition between wild-type (continuous line) and long-period mutant (dashed line) shows coexistence between the two strains for T = 28 h. (B) Coexistence ends after ≈ 8 days of adding 3 minutes of light-time per day. The long-period mutant can win competition as the photoperiod now is closer to its free-running period.

lies in latitude $54^{\circ}48'$. We can see that during the equinoxes, all places receive 12 hours of daylight [13]. Even when changes in photoperiod are not constant over the year and depend on the season, we decide to modify the amount of light per day with fixed steps in order to simplify the equations.

We simulate the seasonal fluctuations in day length by adding or subtracting minutes of lighttime every day to the external LD cycle. For example, if we add 12 minutes of light per day in a LD12:12 cycle, after five days the external cycle of LD has 13 hours of light and 11 of darkness, since the total amount of hours per day is constant. We initiate competition between equal fractions of wild-type strain ($\tau_x = 25h$) and long-period mutant ($\tau_x = 30h$) and equal amounts of light and darkness. In order to mimic experiments in cultures that were diluted and sampled every 8 days [7], we dilute the culture after 8 light-dark cycles by dividing by a factor of 100 the variables N_1 , N_2 and I.

First, we analyzed the case in which the experiments of [7] showed a phase of coexistence. For T = 28, the period of the LD cycle has an intermediate value between the free-running period (FRP) of the two strains and both strains can coexist for



Figure 4: Effect of modulation in light time (30 minutes per day) on the outcome of competition between strain 1 (wild-type, $\tau_x = 25$ h) and strain 2 (long-period mutant, $\tau_x = 30$ h) carried out in two different conditions: (A) LD12:12 and (B) LD15:15. Fraction of strain 1 (left panel) and strain 2 (right panel) are shown as a function of time; red with modulation, so the proportion of L and D changes after each day, and blue with fixed cycles.

a long time. However, when we allowed the days to become longer and the nights shorter, after some days the coexistence was broken, as we show in Fig.3. This is due to the increase in the amount of light hours that benefits the long-period mutant.

In Fig. 4, we show in the left panel the fraction of cells belonging to the wild-type strain as a function of time with fixed LD cycles (red continuous curve) and in the case in which we added 30 minutes of light time each day (blue dashed curve). The first days both curves are similar, but from the second day on, the long-period strain has a FRP closest to the period of the LD cycle. The fraction of wild-type strain starts to decrease and is out-competed. In the right panel, we show the corresponding fraction of long-period mutant cells in the same cases.

Our results show a new way to test competition experimentally. Testing results would be very simple, since the cultures do not need to be diluted. In fact, as shown in Fig. 4, after eight days of competition between the two strains, a difference of about ten percent in the two populations would be needed



Figure 5: Competition between long-period mutant and wild-type strains in a LD12:12 cycle for the same parameters as in Fig. 4, but adding 12 minutes per day the light time. A crossover is observed after 8 days.

in order to verify the theoretical prediction.

Starting from this simple test, we looked for non trivial effects in a longer experiment. We found an interesting effect that can be observed in Fig. 5. In this simulation, we added 12 minutes of light time each day. In the first days, the growth was as expected. The wild-type strain could outcompete the long period mutant strain, since the external cycle was LD12:12. But after eight days, when the day was longer than 13 hours, a crossover was observed. The mutant strain started to win the competition because its endogenous period was closer now to the external cycle. This effect could also be tested experimentally but in this case the dilution of the culture every 8 days would be needed.

IV. Conclusions

The mechanisms underlying the enhancement of reproductive fitness remain still unknown. Despite the fact that numerous models have been tested, each has some evidence that supports it and none can be excluded at this time [12]. In this work, we used a diffusible inhibitor model, so our predictions in the growth rates changes could be useful to test the validity of this mechanism.

Our study is motivated by fluctuations in the day

length throughout the year which are reflected in organisms behavior. We studied how these fluctuations affect the competition between different strains of cyanobacteria. We found non-trivial effects which could be tested experimentally. In the first case, we determined the composition of two strains under competition after eight days when the light is modulated. The prediction of these numerical simulations can be tested in a simple experiment where no dilution is needed. We also propose a second experiment where dilution in the cultures is necessary, which allows for a non trivial effect such as a crossover to be observed.

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