On the impact of the stress situation on the optical properties of WSe$_2$ monolayers under high pressure

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We have studied the optical properties of WSe$_2$ monolayers (ML) by means of photoluminescence (PL), PL excitation (PLE) and Raman scattering spectroscopy at room temperature and as a function of hydrostatic pressure up to ca. 12 GPa. For comparison, the study comprises two cases: A single WSe$_2$ ML directly transferred onto one of the diamonds of the diamond anvil cell and a WSe$_2$ ML encapsulated into hexagonal boron nitride (hBN) layers. The pressure dependence of the A and B exciton, as determined by PL and PLE, respectively, is very different for the case of the bare WSe$_2$ ML and the hBN/WSe$_2$-ML/hBN heterostructure. Whereas for the latter the A and B exciton energy increases linearly with increasing pressure at a rate of 3.5 to 3.8 meV/GPa, for the bare WSe$_2$ ML the A and B exciton energy decreases with a coefficient of -3.1 and -1.3 meV/GPa, respectively. We interpret that this behavior is due to a different stress situation. For a single ML the stress tensor is essentially uniaxial with the compressive stress component in the direction perpendicular to the plane of the ML. In contrast, for the substantially thicker hBN/WSe$_2$-ML/hBN heterostructure, the compression is hydrostatic. The results from an analysis of the pressure dependence of the frequency of Raman active modes comply with the interpretation of having a different stress situation in each case.

I. Introduction

Monolayers (MLs) of group-VI transition metal dichalcogenides (TMDs), MX$_2$ with M=Mo, W and X= S, Se, Te, have emerged as fascinating two-dimensional (2D) semiconductors due to remarkable properties that differ from the bulk. For example, MLs possess a direct band gap located at the K points of the hexagonal Brillouin zone [1, 2]. Electron-hole pairs are also strongly bound by Coulomb interactions giving rise to robust excitons with binding energies of several hundreds of meV [3]. Due to the lack of inversion symmetry in the ML, both spin and K valley degrees of freedom can be controlled using chiral optical selection rules [4]. Finally, the strong spin-orbit coupling is responsible for large splittings in both valence and conduction band with several hundreds and tens of meV at the K points, respectively. This gives rise to a large variety of optically bright and dark excitons, governing the optical properties from cryogenic to room temperature. Bright excitons involving the
first valence band are called A excitons, whereas those involving the second valence band are called B excitons. Dark excitons can be optically inactive due to several reasons. The most studied ones are the spin-forbidden dark excitons which have been identified experimentally in WSe$_2$ and WS$_2$ [5–9]. Momentum mismatch (indirect) excitons composed of electron and hole residing in different K valleys have also been predicted but a clear experimental identification is still lacking. Band structure calculations within density functional theory (DFT) have shown that conduction band minima at the Q points can be a few tens of meV above the K valleys in tungsten-based MLs [10]. Because the effective mass at the Q points is expected to be larger than that at the K points, an indirect exciton composed of an electron in a Q valley and a hole in a K valley may have larger binding energy than a direct bright exciton with electron and hole both residing in the K valley. These indirect excitons may give rise to photoluminescence (PL) emission through phonon assisted process as suggested in Ref. [11].

High pressure methods combined with optical spectroscopy have demonstrated to be a powerful tool to tune the band structure and optical properties of semiconductors in general [13]. Because the bands at different points of the Brillouin zone shift in energy with different pressure coefficients, high pressure experiments can be used to distinguish between k-space direct and indirect transitions. As far as truly two-dimensional (2D) TMD materials are concerned, there are already several reports on the dependence on hydrostatic pressure of the emission and vibrational properties of monolayers of MoS$_2$ [14–18], WSe$_2$ [19] and WS$_2$ [20]. The results, however, are surprisingly contradictory. All studies were performed on MLs transferred or deposited on SiO$_2$/Si wafers, except for the work of Ref. [20], in which authors also looked at the pressure behavior of the ML directly on the diamond anvil surface. We have conducted high-pressure optical-spectroscopy experiments on WSe$_2$ MLs on the diamond anvil and encapsulated by hBN layers for comparison. The encapsulation of TMD MLs using hexagonal boron nitride (hBN) layers contributes much to the preservation of the physical properties of the ML. In fact, narrower PL linewidths have been reported for hBN encapsulated MLs. In this work, we show that different stress situations hold in the two samples, being fully hydrostatic for the hBN/WSe$_2$-ML/hBN heterostructure but uniaxial for the bare ML. This has direct impact on sign and magnitude of the pressure coefficient of the A and B excitons, for example.

II. Experimental details

For the high pressure experiments, the samples are mechanically exfoliated onto the surface of one of the diamond anvils of the high pressure cell (DAC). We thus transferred onto the diamond surface using a polydimethylsiloxane (PDMS) stamp either a WSe$_2$ flake containing some bulk and few-layers parts as well as the desired single monolayer or a hBN/ML/hBN van der Waals (vdW) heterostructure. The latter were fabricated by mechanical exfoliation of bulk WSe$_2$ (commercially available) and hBN crystals [21]. A first layer of hBN is mechanically exfoliated onto a freshly cleaned diamond. The deposition of the subsequent WSe$_2$ ML and the second hBN capping layer is obtained by repeating this procedure. The left panel of Fig. 1 illustrates the result of loading the DAC with bare ML sample.

The high-pressure photoluminescence and micro-Raman scattering measurements were performed at room temperature employing a gasketed diamond anvil cell. A 4:1 methanol/ethanol mixture was used as pressure transmitting medium and a ruby sphere for pressure calibration [22]. The photoluminescence (PL) spectra were excited with the
ingly, with increasing pressure, the A-exciton exits the conduction band and the top of the valence band and occurs between states with the same spin of a single monolayer such emission is direct in nature. Only for a half maximum (FWHM), which corresponds to the energy of the B-exciton, involving holes of the second valence band. A representative PLE spectrum (closed symbols) is displayed in Fig. 3 for the case of the bare WSe$_2$ ML. Each data point of the PLE spectrum corresponds to the energy of the tunable laser used for excitation and the integrated intensity of the A-exciton PL peak, normalized by the incident laser power at the tuned wavelength. The PLE spectra exhibit essentially two features: a kind of excitonic absorption edge associated with the B-exciton and a peak-like feature corresponding to a high-energy critical point (CP) in the joint density of states of a WSe$_2$ ML [23]. Changes in the PLE lineshapes under pressure were analyzed using a fitting function [24] (solid gray curve in Fig. 3), which consists of two components (dash-dotted red curves). The CP feature could be well described by a Gaussian, whereas for the B-exciton we considered a series of Gaussian peaks accounting for the discrete energy spectrum [25] and the analytical expression derived for the exciton continuum in Ref. [26]. Figure S2 of the Supplementary Material shows a representative PLE spectrum for the encapsulated WSe$_2$ ML.

To analyze the PL spectra of the WSe$_2$ MLs, we used a Gaussian-Lorentzian cross-product function for describing the main peak which is ascribed to the A-exciton recombination. This function is a useful simplification of a Voigt function, which corresponds to the mathematical convolution of a Lorentzian, to account for the natural lineshape due to spontaneous emission, and an inhomogeneously broadened Gaussian, accounting for a normal distribution of exciton energies. From these lineshape fits to the PL spectra we were able to extract the energy $E_1$ of the ground state of the excitonic discrete spectrum corresponding to the A-exciton, whereas from the lineshape fits of the PLE spectra we obtained the $E_1$ energy of the B-exciton.
Figure 2: Normalized PL spectra measured at room temperature and as a function of pressure with 488-nm excitation (a) for the bare WSe$_2$ ML and (b) for the hBN/WSe$_2$-ML/hBN vdW heterostructure. The sharp line at 1.58 eV corresponds to the spurious signal from the 785 nm laser.

counterpart [24]. Both ground state energies are plotted as a function of pressure for the bare WSe$_2$ ML and the hBN/WSe$_2$-ML/hBN heterostructure in Figs. 4a,b. Both excitons behave essentially the same under pressure. This means that their energy separation of ca. 425 meV, determined by spin-orbit interaction and an eventual difference in exciton binding energies, is fairly insensitive to pressure [27].

Strikingly, the behavior of the A,B-excitons of the bare and encapsulated WSe$_2$ ML is opposite. Whereas for the hBN/WSe$_2$-ML/hBN heterostructure both exciton energies increase linearly with increasing pressure with a coefficient of 3.5-3.8 meV/GPa, for the bare WSe$_2$ ML the excitons decrease in energy with a slope of -3.1 and -1.3 meV/GPa for the A- and B-exciton, respectively. Comparing with the available literature data, the pressure coefficient of the A-exciton determined here for the encapsulated WSe$_2$ ML is roughly one order of magnitude smaller than the one reported for a single ML of MoS$_2$ (20 meV/GPa [14], 30
meV/GPa [15], 40 meV/GPa [16], 50 meV/GPa [17], WS\textsubscript{2} (32 meV/GPa [19]) and WS\textsubscript{2} (20 meV/GPa [20]). All these data were obtained for monolayers on Si/SiO\textsubscript{2} substrates, where the oxide layer was fairly thick, ranging between 200 and 300 nm. In the work of Han et al. [20], the same experiment is reported for a WS\textsubscript{2} ML exfoliated directly onto the diamond and a much smaller pressure coefficient is found (10 meV/GPa). In the next section, we suggest a possible way to explain such a large disparity in the high pressure results concerning the excitonic properties of single MLs on the basis of a close inspection of the stress-strain relations.

ii. Stress-strain relations for different stress situations

First of all, we have to define the physical system for consideration of its stress/strain situation inside the DAC. It is a common practice to include the substrate supporting the 2D system, provided that adhesion forces between 2D sample and substrate are important. In this respect, we note that the conventional adhesion, corresponding to the tendency of two materials to cling to one another by van der Waals (vdW) forces is not relevant for high pressure experiments. The net vdW adhesion (attractive) force is perpendicular to the surfaces in contact and is proportional to the contact surface. Inside the diamond anvil cell (DAC), however, the substrate (or the diamond) will transmit the same pressure to the sample as it does the pressure transmitting medium, irrespective of the magnitude of the vdW adhesion force. This is just a requirement of the static equilibrium condition. In contrast, a “lateral” adhesion force acts solely in-plane, as is associated with the gliding of one object on a substrate. These lateral forces are typically much weaker than normal adhesion forces. An important exception for which lateral adhesion become significant concerns the case of a rough substrate surface (rippled) and a sample (a thin membrane) showing certain degree of conformation to the substrate surface (see Ref. [28]). This can drive the transmission of in-plane strain (tensile or compressive) from the substrate to the sample, as pointed out by D. Machon et al. [29], being in principle relevant for high pressure experiments, mainly when substrate and sample exhibit different bulk modulus, i.e., different compressibility.

It has been shown [28] that a thin membrane characterized by a bending rigidity \( C \) would be conformal to a rippled surface with a curvature \( \kappa_g \) and an adhesion energy (contact surface potential) \( \gamma \), depending on the values adopted by a dimensionless parameter \( \alpha = \sqrt{\frac{\gamma}{\kappa_g}} \). Here \( \kappa_g = \sqrt{\frac{2}{n}} \) is the equilibrium curvature of the membrane, which is determined by the ratio of the adhesion energy and the bending rigidity of the membrane. When \( \alpha \geq 1 \) the membrane is expected to adhere well to the surface, whereas for \( \alpha \ll 1 \) the membrane cannot adapt to the rippled surface and detaches from it being non-conformal. For the case of a 2D system with \( n \) layers, the bending rigidity depends on \( n \), such that \( C_n \) increases sharply for an increasing number of layers. Thus, \( \alpha \) is expected to decrease with increasing \( n \). In fact, from the analysis of the Raman data regarding the in-plane strain transferred from a Si/SiO\textsubscript{2} substrate to single, bilayer, and multi-layer graphene, it has been inferred that for \( n > 2 \) the 2D system looses its adhesion due to the enhanced rigidity of the multilayers [29–31]. Moreover, in the work of Alencar et al. [18] on the pressure behavior of MoS\textsubscript{2} monolayers on Si/SiO\textsubscript{2} substrates, it was argued that the unbinding of the transition metal dichalcogenide layer from the substrate can already occur for a single layer, because it has a much higher bending modulus than graphene [32]. As a matter of fact, they observe a splitting of the Raman modes of the MoS\textsubscript{2} ML, which is ascribed to the presence of regions with low and high conformation of the ML to the substrate, i.e. regions with different in-plane strain, affecting the frequency of the optical phonons. Concerning our case of having the 2D systems directly transferred onto one on the diamond anvils, we can assume that the thickness and much rigid hBN/WSe\textsubscript{2}-ML/hBN sandwich does not adhere to the diamond. In the case of the WSe\textsubscript{2} monolayer, since we do not observe any splitting neither in the Raman modes (see discussion below) nor in the bright excitonic luminescence (PL), we can also assume that a situation of low conformation applies. Taking all the mentioned facts together, we are led to the conclusion that adhesion effects are not relevant for the proper interpretation of our experimental results and, hence, that we do not have to consider the diamond anvil as part of the physical system.
Figure 4: Ground state energy $E_1$ of the A and B-exciton as a function of pressure (a) for the bare WSe$_2$ ML and (b) for the hBN/WSe$_2$-ML/hBN vdW heterostructure. Lines represent least-squares fits to the data points. Numbers in parentheses represent error bars.

Let us consider that our 2D system corresponding either to the bare WSe$_2$ ML or the hBN/WSe$_2$-ML/hBN vdW heterostructure is well described just as a thin slab of thickness $d$ inside the DAC, as sketched in Fig. 5. For a sufficiently thick slab, the stress situation would be hydrostatic ($\Delta P = 0$). Our ansatz is that for vanishing thickness a departure from the strictly hydrostatic situation would gradually develop. Below a certain critical value, the in-plane stress components will decrease with decreasing thickness by a certain amount $\Delta P$. The reason is that for a vanishing slab cross section the molecules of the pressure medium are unable to transmit any momentum to the slab in the in-plane directions. In the limit of vanishing thickness $d$ (a graphene ML, for example), the in-plane components of the stress tensor would also vanish ($\Delta P = P$).

Although TMD monolayers belong to the $D_{3h}$ space group, from the point of view of their elastic properties it is a good approximation to use an elastic-stiffness tensor with cubic symmetry, i.e., $C_{13} \approx C_{11}$ and $C_{12} \approx C_{12}$ [33]. Please, note that it is not correct to take the bulk values for $C_{13}, C_{12}$, because they are much smaller than for a ML due to inclusion of the weak vdW interlayer interactions. Under these assumptions (see also discussion in the Supplementary Material), we have derived the strain-tensor components $\epsilon_{ij}$ and relative volume change $\Delta V$ for the general stress situation of the slab in Fig. 5:

\begin{align}
\epsilon_{xy} & = -\frac{P}{3B_0} + \frac{C_{11}}{C_{11} - C_{12}} \frac{\Delta P}{3B_0}, \\
\epsilon_z & = -\frac{P}{3B_0} - \frac{2C_{12}}{C_{11} - C_{12}} \frac{\Delta P}{3B_0}, \\
\frac{\Delta V}{V} & = -\frac{P}{B_0} + \frac{2\Delta P}{3B_0},
\end{align}

where

$$B_0 = \frac{1}{3} (C_{11} + 2C_{12})$$

is the “bulk modulus” of the monolayer and the minus sign of the compressive pressure is explicitly written in the equations, such that $0 \geq \Delta P \geq P$. After Eqs. (1) to (3), the usual hydrostatic case corresponds to having $\Delta P = 0$, for which all three strain tensor components are the same and compressive ($\epsilon_{xy} = \epsilon_z = \epsilon^{\text{hydro}}_{xy}$). This occurs for the several monolayers thick hBN/WSe$_2$-ML/hBN heterostructure. On the contrary, an effectively uniaxial stress situation sets in for $\Delta P = P$. In this case, a compressive stress $-P$ is applied from both sides and perpendicular to the plane of the slab, whereas the in-plane strain is tensile ($\epsilon^{\text{uniax}}_{xy} = -\frac{C_{12}}{C_{11} - C_{12}} \cdot \epsilon_{xy}^{\text{hydro}}$). We believe that this situation of highly, if not pure, uniaxial stress does apply for the bare WSe$_2$ ML case, as we argue further below when discussing the Raman results. As a consequence, the sign of the linear pressure coefficient of the A and B-exciton energy changes from positive
to negative for the bare ML as compared to the encapsulated one because for the former the in-plane strain is tensile rather than compressive. Furthermore, for all literature data, the stress situation corresponding to a ML on top of a SiO$_2$/Si substrate is much more complicated. The bulk modulus of the silicon oxide is about one third of that of Si. As discussed in detail in the Supplementary Material, a thick SiO$_2$ layer epitaxially attached to Si will be strongly deformed when hydrostatic pressure is applied, due to the large biaxial tensile stress that the much thicker and less compressive Si exerts on the oxide layer, which under pressure tends to compress three times more than Si. As recognized in Ref. [20], the large deformation of the Si oxide layer introduces an extra strain of the TMD monolayer, which might be the reason for the observation of much higher pressure coefficients for the A,B-excitons.

![Figure 5: Schematic representation of the stress situation inside the DAC for a slab of thickness d. The stress tensor can depart from hydrostatic ($\Delta P \neq 0$), if d $\to$ 0.](image)

iii. Raman scattering under pressure

The dominant first-order Raman active modes of bulk 2H-WSe$_2$ are the one with A$_{1g}$ symmetry, which involves atomic displacements in the direction perpendicular to the layers, and the ones with E$_{2g}$ symmetry, for which the atomic displacements are in-plane [34]. For a single monolayer, the corresponding Raman allowed modes with totally similar eigenvectors as for the bulk are the A$'_{1}$ and E$'$ modes. In WSe$_2$ both mode types possess very similar frequencies and in Raman spectra, both overlap with a very strong signal associated with second-order scattering processes involving two LA phonons (see representative Raman spectra in Figs. S4a-4d of the Supplementary Material). Nevertheless, the Raman signal of the A$_{1g}$ and A$'_{1}$ modes can be resonantly enhanced by tuning the laser wavelength to match the A-exciton energy $E_1$ [34,35]. Near-resonance conditions are attained for bulk WSe$_2$ and the ML with the red 633 nm laser line and the infrared (IR) 785 nm line, respectively. The reason for the resonant behavior is that in TMDs the A-exciton wavefunction contains a large weight from $d^2_z$ orbitals of the metal atoms. This makes the A-exciton energy sensitive to movements of the metal atoms in the direction perpendicular to the layers, as is the case for the eigenvectors of the phonon modes with A symmetry. The non-resonant modes with E symmetry are better seen with blue excitation (488 nm) due to the $1/\omega^4$ prefactor in the Raman cross section. In the following, we show that by comparing the pressure coefficients of the Raman active modes obtained for the bulk and the encapsulated and bare monolayer, we are able to infer a different stress situation for the latter.

Figure 6a shows the results of the Raman measurements as a function of pressure for the modes with A symmetry measured with IR excitation for the hBN/WSe$_2$-ML/hBN heterostructure and a piece of bulk WSe$_2$ which was transferred onto the diamond together with the monolayer. Both slopes are within experimental uncertainty identical, which speaks for a fully hydrostatic compression of the encapsulated monolayer. In contrast, the pressure dependence of the Raman modes with E symmetry of the bare and encapsulated MLs is compared in Fig. 6b. Strikingly, the slope for the bare WSe$_2$ ML is a factor 1.28 smaller than the one of the encapsulated ML. We note that for pure uniaxial compression of a cubic crystal like Si [36] a reduced pressure coefficient by roughly a factor 1.5 is expected for the Raman modes with displacements in the plane perpendicular to the stress. This is just a consequence of the tensile character of the in-plane strain when the material is uniaxially compressed in the perpendicular direction. We are thus led to the conclusion that for the bare ML the stress situation which is most likely established inside the DAC is almost purely uniaxial.
Figure 6: Comparison of the pressure dependence of first-order Raman active modes: (a) The $\text{A}_1g$ mode bulk WSe$_2$ and the $\text{A}'_1$ of the hBN/WSe$_2$-ML/hBN heterostructure measured with 785 nm excitation and (b) the $\text{E}'$ mode of the bare WSe$_2$ ML and hBN/WSe$_2$-ML/hBN heterostructure. Lines represent least-squares fits to the data points and numbers in parentheses represent error bars.

IV. Conclusions

In summary, we have performed a comparative study of the pressure dependence of the optical transition energies corresponding to the radiative recombination of the A and B-excitons for a bare WSe$_2$ ML and a hBN/WSe$_2$-ML/hBN heterostructure, both transferred onto one of the diamonds of the DAC. We have found that for the encapsulated WSe$_2$ ML the energy of both excitons increases with pressure with a relatively small slope of 3.5 to 3.8 meV/GPa, whereas for the bare ML both excitons decrease in energy. These results are at odds with available literature data which show much larger and positive pressure coefficients for a single WSe$_2$ monolayer and other truly 2D TMD materials. It is important to note that the literature data were almost exclusively obtained for monolayers deposited or transferred onto a thick SiO$_2$ layer on top of a Si wafer. To explain the observed discrepancies between the different high pressure experiments on 2D TMDs, we have proposed a revision of the stress situation in each particular case, which depends principally on the effective thickness of the slab being pressurized in the DAC. Here, we propose that for the bare single monolayer (case of vanishing thickness) the stress situation is better described by using an uniaxial stress tensor, whereas for the much thicker hBN/WSe$_2$-ML/hBN heterostructure conventional hydrostatic conditions can be assumed. Our Raman results, obtained simultaneously with the PL and PLE data in each case, speak in favor of such an interpretation. We believe that our findings will have significant impact on future high pressure work on truly 2D material systems like graphene, TMDs, BN, and other layered materials, for the assessment of the stress situation appears to be crucial for the correct interpretation of the experimental results.

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